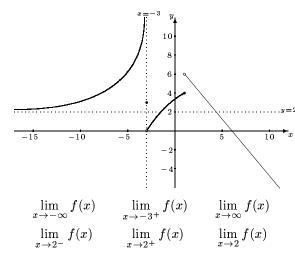


- 1. Determine each of the following limits if possible. If the limit does not exist explain and/or use ∞ or $-\infty$ as appropriate. (Show your work.)
 - (a) $\lim_{x \to 0} \frac{\sin^2 x}{2x}$
- (b) $\lim_{x \to -1} \frac{x^2 + 2x + 1}{x^2 x 2}$
- (c) $\lim_{x \to 6} \frac{\sqrt{6-x}-2}{2-x}$ (d) $\lim_{x \to 3^-} \frac{|x-3|}{(x-3)^2}$
- (e) $\lim_{x \to \infty} \frac{3x^3 + 4x + 2}{5 x x^3}$
- (f) Use the graph of f given below to find the limits.



2. Use the definition of derivative to find f'(x) if

$$f(x) = \frac{1}{1+x}.$$

3. Use the definition of continuity at a point to determine

$$f(x) = \begin{cases} x - 4 & \text{if } x \leqslant 2\\ x^2 - 6 & \text{if } x > 2 \end{cases}$$

is continuous at x=2.

4. Find the value of k such that

$$g(x) = \begin{cases} \frac{x^2 - 9}{x - 3} & \text{if } x \neq 3\\ k & \text{if } x = 3 \end{cases}$$

is continuous at x = 3.

5. Find the derivative of the following functions. Do not simplify your answers.

(a)
$$y = 3x^2 - \frac{4}{\sqrt[3]{x}} + \pi$$
 (b) $f(x) = \frac{3x - 5}{\sqrt{x} + 1}$

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$$f(x) = \frac{3x-5}{\sqrt{x}+1}$$

(c)
$$y = 5\sec^2(3x) + \tan(3x^2)$$

- (d) $g(x) = e^{-x^2} \ln(1+x^2)$ (e) $y = \sqrt{x^2 a^2}$ (where a is constant)
- 6. Use logarithmic differentiation to find $y = (x^2 + 1)^{\frac{1}{x}}$. Do not simplify your answer.
- 7. Let $f(x) = x^2 e^{2x}$.
 - (a) Determine if f'(x) and simplify.
 - (b) Determine any values of x where the tangent line to the graph of f is horizontal.
- 8. If $y = x^{\frac{1}{2}} + x^{-\frac{1}{2}}$, find y'' and write in simplified form as a single fraction without negative exponents.
- 9. Given $x^2 + y^2 = 3y$.
 - (a) Find $\frac{dy}{dx}$ at the point $(-\sqrt{2}, 2)$. (b) Find an equation for the tangent line to the curve
 - at $(-\sqrt{2}, 2)$.
- 10. Determine the absolute maximum and absolute minimum values of $f(x) = 12x - x^3$ on [0, 4].
- 11. Given $f(x) = x^{\frac{2}{3}}(x+5)$,

$$f'(x) = \frac{5(x+2)}{3x^{\frac{1}{3}}}$$
 and $f''(x) = \frac{10(x-1)}{9x^{\frac{4}{3}}}$.

- (a) Find intercepts, relative extrema, and inflection points, if any.
- (b) Use the information in (a) to sketch the graph of f.
- 12. Given: $V = \frac{4}{3}\pi r^3$ (Volume of a balloon formula) S = $4\pi r^2$ (Surface area of a balloon formula).

The volume of a large balloon is decreasing at a constant rate of $50 \text{ ft}^3/\text{min}$.

- (a) How fast is the radius r of the balloon decreasing at the instant the radius is 4 ft?
- (b) How fast is the surface area of S decreasing at the instant the radius is 4 ft?
- 13. Determine the coordinates of the point on the graph of $y = \frac{6}{x}$, x > 0 which is closest to the origin by minimizing the square of the distance between the origin and a typical point on the graph.
- 14. Find the following integrals:

(a)
$$\int \left(2x - 1 + \frac{3}{x} - \frac{4}{x^2}\right) dx$$
 (b) $\int_{-\frac{\pi}{6}}^{\frac{\pi}{6}} \frac{1}{2} \cos \vartheta \, d\vartheta$ (c) $\int (e^x + x^e) \, dx$ (d) $\int_{-\frac{\pi}{6}}^{2} 3x(x^2 + 5) \, dx$

15. Find the area of the region enclosed by $y = x^2 + \sec^2 x$ and y=0 from x=0 to $x=\frac{\pi}{4}$.